

Perform the indicated operations and reduce to lowest terms.

1) $\frac{12a^2b^4}{16a^5bc^2}$

2) $\frac{4x^2y^3}{16xy^5}$

3) $\frac{32a^2}{7xb^2} \cdot \frac{21x^2b^4}{8a^3}$

4) $24a^2b^3 \cdot \frac{16x^3b}{9a}$

5) $\frac{38xy^2z}{81a^2b^3} \div \frac{19ac^2}{27y^2}$

6) $\frac{4x^2y^3z^2}{12xy^4} \div \frac{24xy^5}{16xy}$

7) $\frac{32x^2c}{12a^2b} \cdot \left(\frac{17a^2x^2}{34b^2c} \cdot \frac{16x}{9a} \right)$

8) $\frac{32x^2c}{12a^2b} \div \left(\frac{17a^2x^2}{34b^2c} \cdot \frac{16x}{9a} \right)$

9) $\frac{4x+8}{3x-6} \cdot \frac{6x-12}{8x+16}$

10) $\frac{x-3}{2x^2-5x-3} \cdot (8x+4)$

11) $(8x+4) \div \frac{x-3}{2x^2-5x-3}$

12) $\frac{2x^2-5x-12}{3x^2-11x-4} \cdot \frac{3x^2-14x-5}{2x^2-7x-15}$

$$13) \frac{2a^2 + ab - 3b^2}{a^2 - b^2} \cdot \frac{2a - 2b}{2a^2 + 5ab + 3b^2}$$

$$14) \frac{9x^2 - 9x + 2}{2x - 6x^2} \cdot \frac{6x^3}{3x - 2}$$

$$15) \frac{x^2 - y^2}{y^3x - x^3y} \cdot (x^2 + 2xy + y^2)$$

$$16) \frac{4x^2 - 4x - 3}{8x + 4x^2} \cdot \frac{16x^2}{4x^2 - 6x}$$

$$17) \frac{6x^2 + x - 2}{4x^2 - 8x + 3} \cdot \left(\frac{x-1}{3x+2} \cdot \frac{8x-12}{2x-2} \right)$$

$$18) \frac{9y^2 + 9y + 2}{3y^2 - 2y - 1} \div \left(\frac{y-1}{3y^2 + 4y + 1} \cdot \frac{3y+2}{y+1} \right)$$

$$19) \frac{3a+2b}{2a^2+3ab} \cdot \frac{2a^2+ab-3b^2}{9a^2-4b^2} \cdot \frac{3a^2b^2-2ab^3}{a-b}$$

$$20) \frac{4x^2-12x+9}{8x^3-27} \div \frac{4x^2-9}{12x^3+18x^2+27x}$$

Answers: 1) $\frac{3b^3}{4a^3c^2}$ 2) $\frac{x}{4y^2}$ 3) $\frac{12xb^2}{a}$ 4) $\frac{128ab^4x^3}{3}$ 5) $\frac{2xy^4z}{3a^3b^3c^2}$ 6) $\frac{2xz^2}{9y^5}$ 7) $\frac{64x^5}{27ab^3}$

8) $\frac{3bc^2}{a^3x}$ 9) 1 10) 4 11) $4(2x+1)^2$ 12) 1 13) $\frac{2(a-b)}{(a+b)^2}$ 14) $-3x^2$ 15) $-\frac{(x+y)^2}{xy}$

16) $\frac{2(2x+1)}{2+x}$ 17) 2 18) $\frac{(3y+1)(y+1)^2}{(y-1)^2}$ 19) b^2 20) $\frac{2x}{2x+3}$